



# ***Sources of Uncertainty in Gamma Spectrometry***

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# Sources of Uncertainty



## ▶ Presentation Overview

- ◆ **Uncertainties contributing to the total measurement uncertainty**
- ◆ **Cascade Summing Effect**
- ◆ **Unknown sample characteristics**

# Sources of Uncertainty



## ▶ Uncertainties contributing to the total measurement uncertainty (TMU)

### ◆ Statistical measurement uncertainty

- Value may be very different depending on
  - Activity of sample (Count Rate)
  - Counting Time
  - Environmental Background / Other nuclides in sample
- Range:
  - Few percent to 100%

# Sources of Uncertainty



## ▶ Uncertainties contributing to the TMU

### ◆ Calibration (Efficiency) Uncertainty

- 2 different ways of determining the efficiency
  - Calibration source
  - Mathematical calculation, f. ex. by ISOCS / LabSOCS (Canberra)

# Sources of Uncertainty



## ▶ Calibration source

- ◆ Depending on the price of the calibration source, the inherent source uncertainty is in the range of 1 – 5 %
- ◆ Additional: statistical uncertainty of the calibration source measurement
- ◆ The statistical uncertainty mostly can be reduced to a level of 1 – 2 %
- ◆ Summary: The calibration uncertainty is in the range of 2 – 5 or 6%

# Sources of Uncertainty



## ▶ Mathematical Efficiency Calculation

- ◆ Based on Monte Carlo Simulations
- ◆ Range:
  - 4 to 10 % depending on  $\gamma$ - Energy
- ◆ Summary: it looks, as if the uncertainty from mathematical calibrations is higher than the uncertainty from Source calibrations – see later

# Sources of Uncertainty



## ▶ Nuclear Parameters

- ◆ Uncertainty in half live
- ◆ Uncertainty in emission rate
- ◆ Neglegible

## ▶ Uncertainty in Counting time

- ◆ Neglegible

# Sources of Uncertainty



- ▶ **Systematic Uncertainty**
- ▶ **Random Uncertainty**
  - ◆ **Sample Preparation**
  - ◆ **Sample Quantity**



# Sources of Uncertainty



- ▶ All the listed uncertainties are mathematically propagated and result in a Total Measurement Uncertainty (TMU)
- ▶ A TMU of 3 to 5% (or even lower) can be achieved
- ▶ In environmental samples, the TMU is mostly higher: >10%

# Sources of Uncertainty



- ▶ **All the previous topics ignore the Cascade Summing Effect (True Coincidence Summing)**
- ▶ **This effect comes from the fact that many nuclides emit 2 or more gammas within a very short period of time, which are not separated in the detector. This results in the fact, that too few gammas of a specific energy are seen. So, an activity is calculated, which is too low.**
- ▶ **The Cascade Summing Effect depends on**
  - ◆ **The nuclide decay scheme**
  - ◆ **The sample geometry**

# Sources of Uncertainty



- ▶ **Genie-2000 can correct for the effects of Cascade Summing (Cascade Summing Correction: CSC)**
- ▶ **Prerequisites:**
  - ◆ **Knowledge of the detector characteristics, especially of the 'Total Efficiency'**
  - ◆ **Description of the sample geometry**
  - ◆ **Knowledge of the nuclide decay scheme (internally stored in a CSC Library)**

# Sources of Uncertainty



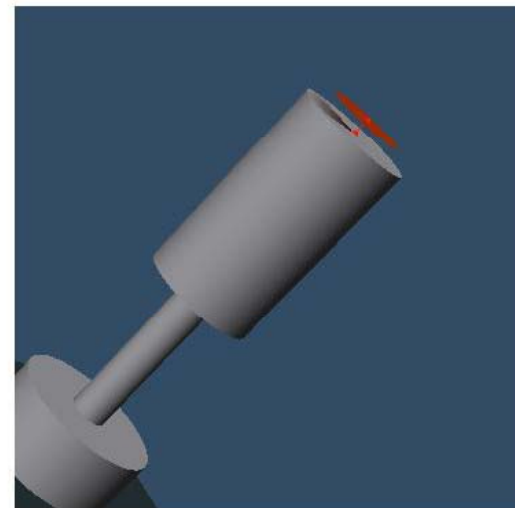
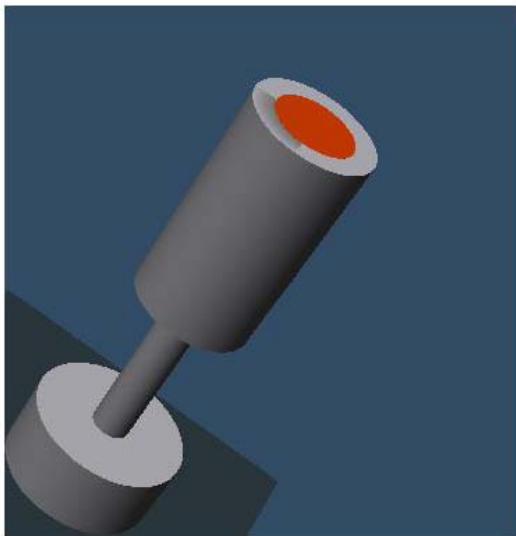
- ▶ **The Total efficiency can be introduced in one of 2 ways:**
  - ◆ Perform a P/T- Calibration and calculate it from this relationship and the known Peak- Efficiency
  - ◆ Calculate it directly based on the so-called detector characterization (Canberra) or on the known detector data (size, etc.) – This method is more precise than the calibration – It is available since version 3.2 (now)
- ▶ **The nuclide data can be imported directly from internationally approved nuclide library (ENSDF)**

# Sources of Uncertainty



## ► Example:

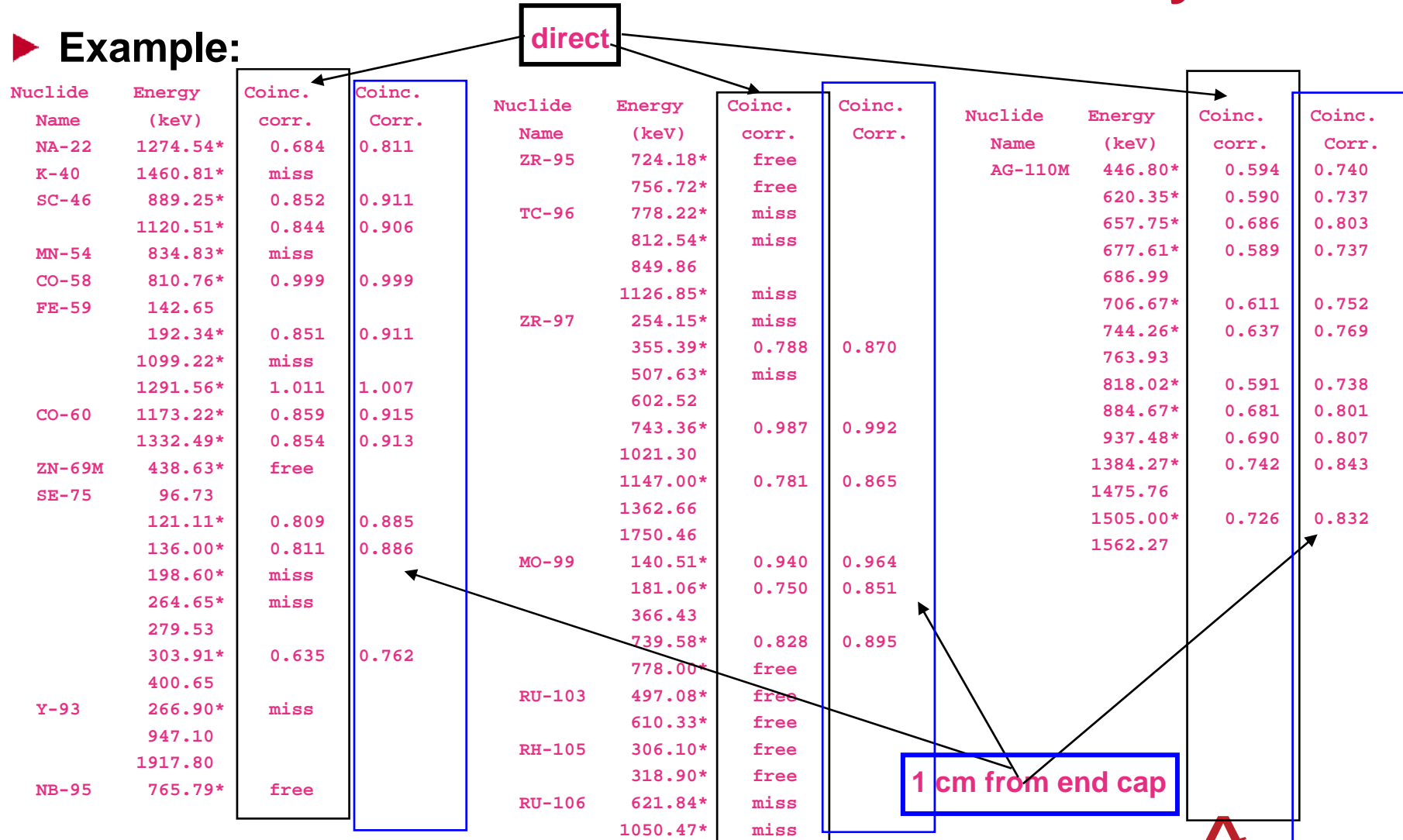
- ◆ Measurement of a filter sample (5cm dia.) , measured directly on top of the end cap and at 10 mm distance
- ◆ Detector: about 30%





# Sources of Uncertainty

## ► Example:



# Sources of Uncertainty



- ▶ **Estimation of Uncertainties for Calibration**
  - ◆ Eff calibration with calibration source: Uncertainty: few percent
  - ◆ Mathematical eff calibration: Uncertainty: 4 to 10 percent
- ▶ **For calibration sources:**
  - ◆ Size of uncertainty only valid, if physical characteristics of the calibration source are identical to those of the real sample
- ▶ **For mathematical calibration:**
  - ◆ This value only applies for the statistical simulation process
- ▶ **Additional uncertainties arise from differences in the source properties**

# Sources of Uncertainty



- ▶ **The source calibration cannot take these differences into account**
- ▶ **The mathematical calibration can do so, if the characteristics are known**



# Sources of Uncertainty



- ▶ **If this is not the case, uncertainties can be determined by**
  - ◆ **ISOCS**
  - ◆ **Uncertainty**
  - ◆ **Estimator**
- ▶ **IUE is based on the ISOCS sample model**
- ▶ **It varies the not well known information and calculates statistical variations of the efficiency curve**

# Sources of Uncertainty



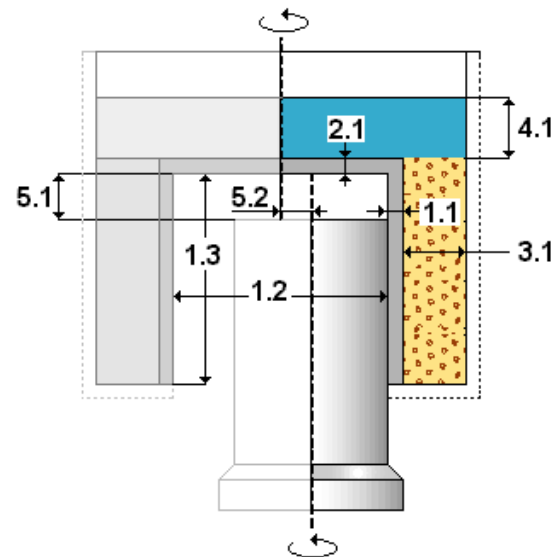
## ► Example:

◆ **Detector: 30%**

◆ **Sample:**

- Marinelli Beaker filled with 1.6 kg of soil
- Wall thickness of beaker: between 1.3 and 3.0 mm
- Density of material between 1.4 and 1.7 g/cm<sup>3</sup>
- Filling height between 110.9 and 127.7 mm (depending on density of material)

General Purpose Marinelli Beaker



# Sources of Uncertainty



## ► Example:

- ◆ Detector: 30%
- ◆ Sample:

Wall thickness

Density of material

Filling height

Variable basic entries

Name der GIS-Da: marinelli-11.gis

Liste von Parametern anzeigen/bearbeiten

Längeneinheiten:  mm  cm  m  in  ft

Verteilungsfunktionen:  gleichfö  dreiseitig  68% V  95% VN  99% VN

Niedrig Hoch

Rückgäng. Bestätigen

| Beschreibung | Element   | aktuell | Niedrig | Hoch | Einheiten | Verteilung  |
|--------------|-----------|---------|---------|------|-----------|-------------|
| Liner_side   | 1.1       | 2       | 1.5     | 3    | mm        | gleichförm. |
| Liner_side   | 1.1       | 2       | 1.5     | 3    | mm        | gleichförm. |
| Liner_side   | 1.2       | 90      |         |      | mm        |             |
| Liner_side   | 1.3       | 58      |         |      | mm        |             |
| Liner_side   | 1.Dichte  | 0.95    |         |      | g/cm3     |             |
| Liner-end    | 2.1       | 2       |         |      | mm        |             |
| Liner-end    | 2.Dichte  | 0.95    |         |      | g/cm3     |             |
| Source-side  | 3.1       | 16      |         |      | mm        |             |
| Source-side  | 3.Dichte  | 1.6     | 1.4     | 1.7  | g/cm3     | gleichförm. |
| Source-side  | 3.RelKonz | 1       |         |      |           |             |
| Source-end   | 4.1       | 53.593  | 50.9    | 67.1 | mm        | gleichförm. |
| Source-end   | 4.Dichte  | 1.6     | 1.4     | 1.7  | g/cm3     | gleichförm. |
| Source-end   | 4.RelKonz | 1       |         |      |           |             |

Zurück... Ende Weiter...

# Sources of Uncertainty



- ▶ Example:
- ◆ Results:

**Status- und Ergebnisanzeige**

Zeit: Startzeit: Mon Aug 10 14:40:52 2009  
 verg. Zeit: 00:01:34  
 Geschätzte Restzeit: 00:01:34

Modelle: Name der GIS-Da: marinelli-1.lgis  
 Vorlagentyp: well\_or\_marinelli\_beaker  
 Min: 1 Max: 1 Fertig: 1 ISOCS-Läufe pro Modell: 9

Berechnung starten/forts. Effizienzerg. sichern

Laufparameter:  
 Endkriterium: % Änderung im arithm. Mittel der Effizienz wenn das letzte Modell hinzugefügt wurde  
 Erforderliche Anzahl von sukzessiven Iteration: 3  
 Energie, keV: <50 50 - 200 200 - 500 >500  
 Konvergenz, %: 1 1 1 1

Liste des Effizienztyps:  
 Effizienz  
 Effizienz\*Masse  
 Effizienz\*Fläche

Genie-Effizienzdateityp:  
 Arithmetisches Mittel der Effizienz und Std.Abw.  
 Geometrisches Mittel der Effizienz und Std.Abw.  
 Unsicherheiten von ISOCS ignorieren  
 Kombiniere Unsicherheiten von ISOCS linear  
 Kombiniere Unsicherheiten von ISOCS quadratisch

ECC-Datei erstellen

Zeige Werte für:  
 Effizienz aller Modellläufe  
 Effizienz jeder einzelnen ISOCS-Berechnung  
 Anteil der Effizienzänderung wenn die variablen Parameter individuell verändert werden

Anteil der Effizienzänderung wenn die variablen Parameter individuell verändert werden- alle Werte konvertiert zu 68% cl [Effizienz]

| Elementb... | Elem... | 45 k... | 60 keV | 80 keV | 100 keV | 150 keV | 200 k... | 300 k... | 500 keV | 700 keV | 1000... | 1400... | 2000 keV |
|-------------|---------|---------|--------|--------|---------|---------|----------|----------|---------|---------|---------|---------|----------|
| Liner_side  | 1.1     | 0.98    | 0.98   | 0.98   | 0.98    | 0.98    | 0.98     | 0.98     | 0.98    | 0.98    | 0.98    | 0.98    | 0.98     |
|             | 1.1     | 1.01    | 1.01   | 1.01   | 1.01    | 1.01    | 1.01     | 1.01     | 1.01    | 1.01    | 1.01    | 1.01    | 1.01     |
| Source-side | 3Dic... | 1.00    | 1.00   | 1.00   | 1.00    | 1.00    | 1.00     | 1.00     | 1.00    | 1.00    | 1.00    | 1.00    | 1.00     |
|             | 3Dic... | 1.00    | 1.00   | 0.99   | 0.99    | 0.99    | 0.99     | 0.99     | 0.99    | 0.99    | 0.99    | 0.99    | 0.99     |
| Source-end  | 4.1     | 0.92    | 0.92   | 0.92   | 0.93    | 0.93    | 0.93     | 0.93     | 0.93    | 0.93    | 0.94    | 0.94    | 0.94     |
|             | 4.1     | 1.02    | 1.02   | 1.02   | 1.02    | 1.02    | 1.02     | 1.02     | 1.01    | 1.01    | 1.01    | 1.01    | 1.01     |
| Source-end  | 4Dic... | 0.98    | 0.98   | 0.98   | 0.98    | 0.98    | 0.99     | 0.99     | 0.99    | 0.99    | 0.99    | 0.99    | 0.99     |
|             | 4Dic... | 1.05    | 1.04   | 1.04   | 1.03    | 1.03    | 1.03     | 1.03     | 1.03    | 1.02    | 1.02    | 1.02    | 1.02     |
|             |         | 1.00    | 1.00   | 1.00   | 1.00    | 1.00    | 1.00     | 1.00     | 1.00    | 1.00    | 1.00    | 1.00    | 1.00     |

Wall thickness

Density of material

Filling height

A stylized, bold, red letter 'A' logo. The letter is composed of thick, solid red strokes. The top bar is horizontal, and the two vertical strokes are slightly angled outwards. A small horizontal stroke crosses the middle of the 'A'.

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